

SPLS, 7 Jun 2023, University of the West of Scotland

ASYNCHRONOUS **OPERATIONS**

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THE **IDEA**

M_1

$$M_1 \rightsquigarrow M_2$$

$$M_1 \rightsquigarrow M_2 \rightsquigarrow M_3$$

$$M_1 \rightsquigarrow M_2 \rightsquigarrow M_3 \rightsquigarrow M_4$$

$$M_1 \rightsquigarrow M_2 \rightsquigarrow M_3 \rightsquigarrow M_4 \rightsquigarrow M_5$$

M_1

$$M_1 \rightsquigarrow M_2$$

$$M_1 \rightsquigarrow M_2 \quad \uparrow_{\text{op}}$$

$$\begin{array}{ccc}
 & \uparrow_{\text{op}} & \downarrow_{\text{res}} \\
 M_1 \rightsquigarrow M_2 & & M_3
 \end{array}$$

$$\begin{array}{ccc}
 & \uparrow_{\text{op}} & \downarrow_{\text{res}} \\
 M_1 \rightsquigarrow M_2 & & M_3 \rightsquigarrow M_4
 \end{array}$$

$$\begin{array}{ccc}
 & \uparrow_{\text{op}} & \downarrow_{\text{res}} \\
 M_1 \rightsquigarrow M_2 & & M_3 \rightsquigarrow M_4 \rightsquigarrow M_5
 \end{array}$$

M_1

$$M_1 \rightsquigarrow M_s$$

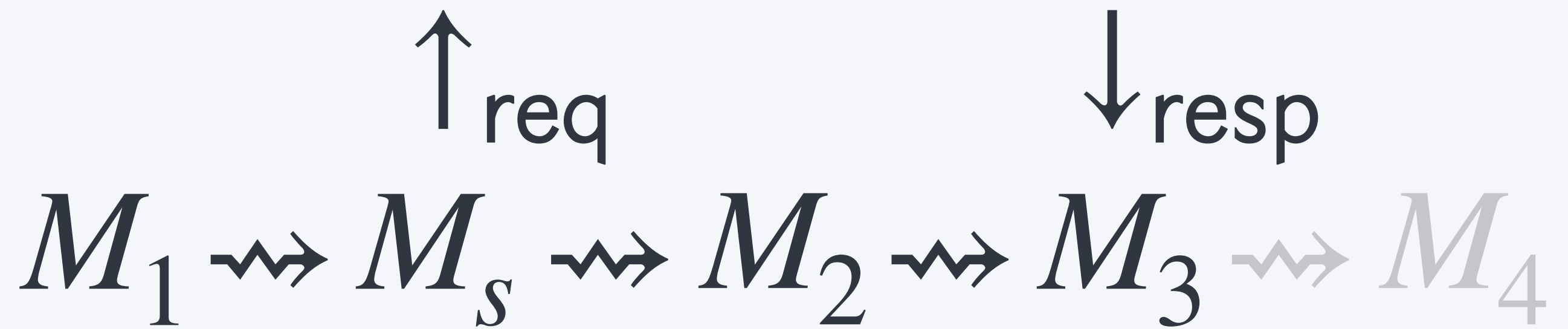
$$M_1 \rightsquigarrow M_s \quad \uparrow_{\text{req}}$$

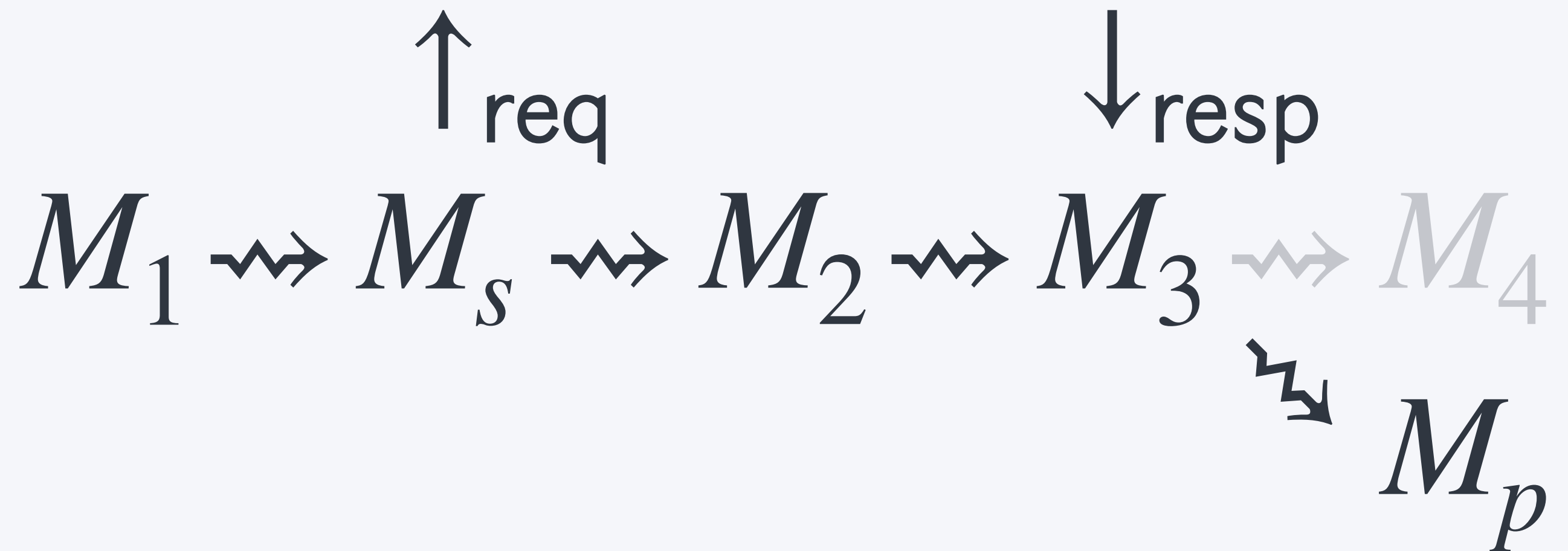
$$\begin{array}{c}
 \uparrow \text{req} \\
 M_1 \rightsquigarrow M_s \rightsquigarrow M_2
 \end{array}$$

$$\begin{array}{c}
 \uparrow \text{req} \\
 M_1 \rightsquigarrow M_s \rightsquigarrow M_2 \rightsquigarrow M_3
 \end{array}$$

$$\begin{array}{c}
 \uparrow_{\text{req}} \\
 M_1 \rightsquigarrow M_s \rightsquigarrow M_2 \rightsquigarrow M_3 \rightsquigarrow M_4
 \end{array}$$

$$\begin{array}{c}
 \uparrow \text{req} \\
 M_1 \rightsquigarrow M_s \rightsquigarrow M_2 \rightsquigarrow M_3 \rightsquigarrow M_4
 \end{array}$$





M_1

$$M_1 \rightsquigarrow M_w$$

$$M_1 \rightsquigarrow M_w$$

$\downarrow \text{req}$

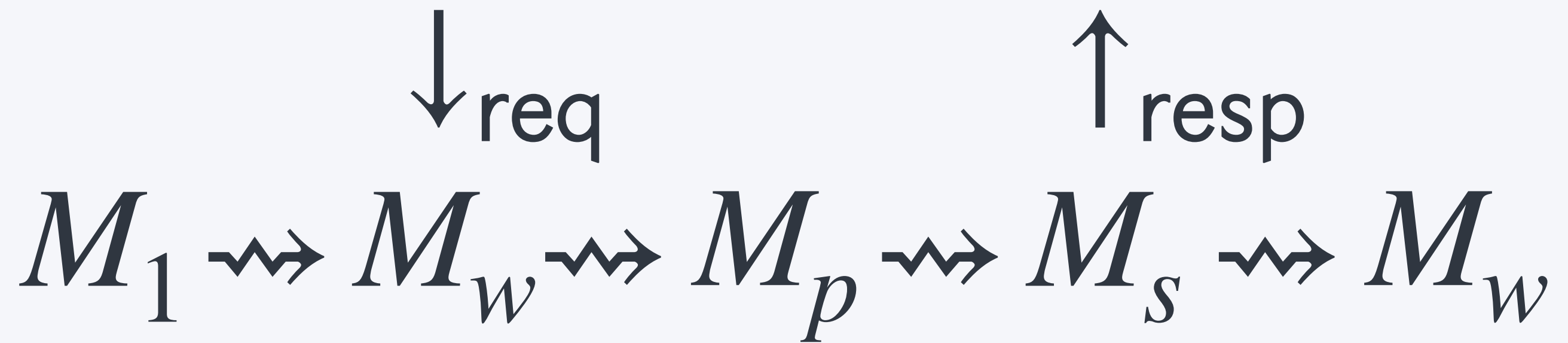
\downarrow req

$$M_1 \rightsquigarrow M_w \rightsquigarrow M_p$$

\downarrow req

$$M_1 \rightsquigarrow M_w \rightsquigarrow M_p \rightsquigarrow M_s$$





M_1

$$M_1 \rightsquigarrow M_2$$

↓ stop

$M_1 \rightsquigarrow M_2$

↓ stop

$$M_1 \rightsquigarrow M_2 \rightsquigarrow M_{w_2}$$

$$\begin{array}{ccccc}
 & & \downarrow \text{stop} & & \downarrow \text{go} \\
 M_1 & \rightsquigarrow & M_2 & \rightsquigarrow & M_{w_2}
 \end{array}$$

$$\begin{array}{ccccc}
 & & \downarrow \text{stop} & & \downarrow \text{go} \\
 M_1 & \rightsquigarrow & M_2 & \rightsquigarrow & M_{w_2} \rightsquigarrow M_2
 \end{array}$$

$$\begin{array}{ccccccc}
 & & \downarrow \text{stop} & & \downarrow \text{go} & & \\
 M_1 & \rightsquigarrow & M_2 & \rightsquigarrow & M_{w_2} & \rightsquigarrow & M_2 \rightsquigarrow M_3
 \end{array}$$

M_1

\uparrow tick
 M_1

$$\begin{array}{c} \uparrow \text{tick} \\ M_1 \rightsquigarrow M_2 \end{array}$$

$$\begin{array}{ccc}
 \uparrow \text{tick} & & \uparrow \text{tock} \\
 M_1 & \rightsquigarrow & M_2
 \end{array}$$

$$\begin{array}{ccccc}
 \uparrow \text{tick} & & \uparrow \text{tock} & & \\
 M_1 & \rightsquigarrow & M_2 & \rightsquigarrow & M_1
 \end{array}$$

$$\begin{array}{ccccc}
 \uparrow \text{tick} & & \uparrow \text{tock} & & \uparrow \text{tick} \\
 M_1 & \rightsquigarrow & M_2 & \rightsquigarrow & M_1
 \end{array}$$

$$\begin{array}{ccccc}
 \uparrow \text{tick} & & \uparrow \text{tock} & & \uparrow \text{tick} \\
 M_1 & \rightsquigarrow & M_2 & \rightsquigarrow & M_1 & \rightsquigarrow & M_2
 \end{array}$$

$$\begin{array}{cccc}
 \uparrow \text{tick} & \uparrow \text{tock} & \uparrow \text{tick} & \uparrow \text{tock} \\
 M_1 \rightsquigarrow M_2 & \rightsquigarrow M_1 & \rightsquigarrow M_2 & \rightsquigarrow M_1
 \end{array}$$

$$\begin{array}{ccccccc}
 \uparrow \text{tick} & & \uparrow \text{tock} & & \uparrow \text{tick} & & \uparrow \text{tock} \\
 M_1 & \rightsquigarrow & M_2 & \rightsquigarrow & M_1 & \rightsquigarrow & M_2 \rightsquigarrow M_1
 \end{array}$$

THE **IDEA**

CORE **CALCULUS**

$\text{fun } (x : X) \mapsto M \quad VW$
 $\text{return } V \quad \text{let } x = M \text{ in } N$

$$(\text{fun } (x : X) \mapsto M) V \rightsquigarrow M[V/x]$$

$$\text{let } x = (\text{return } V) \text{ in } N \rightsquigarrow N[V/x]$$

$$\frac{M \rightsquigarrow N}{\mathcal{E}[M] \rightsquigarrow \mathcal{E}[N]}$$

$$\mathcal{E} ::= [] \mid \text{let } x = \mathcal{E} \text{ in } N \mid \dots$$

demo

CORE **CALCULUS**

$\text{fun } (x : X) \mapsto M \quad VW$
 $\text{return } V \quad \text{let } x = M \text{ in } N$

OUTGOING **SIGNALS**

$\uparrow \text{op}(V, M)$

$$\text{let } x = (\uparrow \text{op } (V, M)) \text{ in } N \\ \rightsquigarrow \uparrow \text{op } (V, \text{let } x = M \text{ in } N)$$

$$\mathcal{E} ::= \dots \mid \uparrow \text{op } (V, \mathcal{E})$$

$$\text{let } x = (\uparrow \text{op } (V, M)) \text{ in } N \\ \rightsquigarrow \uparrow \text{op } (V, \text{let } x = M \text{ in } N)$$

$$\mathcal{E} ::= \dots \mid \uparrow \text{op } (V, \mathcal{E})$$

no bound variable

demo

OUTGOING **SIGNALS**

$\uparrow \text{op}(V, M)$

INCOMING **INTERRUPTS**

$\downarrow \text{op}(V, M)$

$$\downarrow \text{op} (V, \text{return } W) \rightsquigarrow \text{return } W$$

$$\downarrow \text{op} (V, \uparrow \text{op}' (W, M)) \rightsquigarrow \uparrow \text{op}' (W, \downarrow \text{op} (V, M))$$

$$\mathcal{E} ::= \dots \mid \downarrow \text{op} (V, \mathcal{E})$$

demo

INCOMING **INTERRUPTS**

$\downarrow \text{op}(V, M)$

INTERRUPT **HANDLERS**

promise (op $x \mapsto M$) as p in N

$\text{let } x = (\text{promise } (\text{op } y \mapsto M_1) \text{ as } p \text{ in } M_2) \text{ in } N$
 $\rightsquigarrow \text{promise } (\text{op } y \mapsto M_1) \text{ as } p \text{ in } (\text{let } x = M_2 \text{ in } N)$

$\text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \uparrow \text{op}'(V, N)$
 $\rightsquigarrow \uparrow \text{op}'(V, \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$

$\mathcal{E} ::= \dots \mid \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \mathcal{E}$

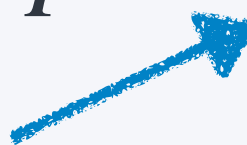
$$\text{let } x = (\text{promise } (\text{op } y \mapsto M_1) \text{ as } p \text{ in } M_2) \text{ in } N$$

$$\rightsquigarrow \text{promise } (\text{op } y \mapsto M_1) \text{ as } p \text{ in } (\text{let } x = M_2 \text{ in } N)$$


$$\text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \uparrow \text{op}'(V, N)$$

$$\rightsquigarrow \uparrow \text{op}'(V, \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$$

$$\mathcal{E} ::= \dots \mid \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \mathcal{E}$$


bound variable 

$\text{let } x = (\text{promise } (\text{op } y \mapsto M_1) \text{ as } p \text{ in } M_2) \text{ in } N$
 $\rightsquigarrow \text{promise } (\text{op } y \mapsto M_1) \text{ as } p \text{ in } (\text{let } x = M_2 \text{ in } N)$


 algebraicity

$\text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \uparrow \text{op}'(V, N)$
 $\rightsquigarrow \uparrow \text{op}'(V, \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$

$\mathcal{E} ::= \dots \mid \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \mathcal{E}$


 bound
variable

$\text{let } x = (\text{promise } (\text{op } y \mapsto M_1) \text{ as } p \text{ in } M_2) \text{ in } N$
 $\rightsquigarrow \text{promise } (\text{op } y \mapsto M_1) \text{ as } p \text{ in } (\text{let } x = M_2 \text{ in } N)$

← algebraicity

$\text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \uparrow \text{op}'(V, N)$
 $\rightsquigarrow \uparrow \text{op}'(V, \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$

← commutativity

$\mathcal{E} ::= \dots \mid \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \mathcal{E}$

bound variable →

$\downarrow \text{op} (V, \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$

$\rightsquigarrow \text{let } p = M[V/x] \text{ in } \downarrow \text{op} (V, N)$

$\downarrow \text{op}' (V, \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$

$\rightsquigarrow \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \downarrow \text{op}' (V, N)$

$\downarrow \text{op} (V, \text{promise} (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$

$\rightsquigarrow \text{let } p = M[V/x] \text{ in } \downarrow \text{op} (V, N)$

"handling"

$\downarrow \text{op}' (V, \text{promise} (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$

$\rightsquigarrow \text{promise} (\text{op } x \mapsto M) \text{ as } p \text{ in } \downarrow \text{op}' (V, N)$

INTERRUPT **HANDLERS**

promise (op $x \mapsto M$) as p in N

AWAITING

PROMISES

$\langle V \rangle$

await V until $\langle x \rangle$ in M

await $\langle V \rangle$ **until** $\langle x \rangle$ **in** $M \rightsquigarrow M[V/x]$

let $x =$ (**await** V **until** $\langle y \rangle$ **in** M) **in** N
 \rightsquigarrow **await** V **until** $\langle y \rangle$ **in** (**let** $x = M$ **in** N)

$\downarrow \text{op}$ (V , **await** W **until** $\langle x \rangle$ **in** M)
 \rightsquigarrow **await** W **until** $\langle x \rangle$ **in** $\downarrow \text{op}$ (V, M)

await $\langle V \rangle$ **until** $\langle x \rangle$ **in** $M \rightsquigarrow M[V/x]$

let $x = (\text{await } V \text{ until } \langle y \rangle \text{ in } M) \text{ in } N$

\rightsquigarrow **await** V **until** $\langle y \rangle$ **in** (**let** $x = M$ **in** N)

 algebraicity

$\downarrow \text{op}$ (V , **await** W **until** $\langle x \rangle$ **in** M)

\rightsquigarrow **await** W **until** $\langle x \rangle$ **in** $\downarrow \text{op}$ (V , M)

 "handling"

demo

AWAITING

PROMISES

$\langle V \rangle$

await V until $\langle x \rangle$ in M

TYPES

$$\Gamma \vdash V : X$$
$$\Gamma \vdash M : X! \mathcal{C}$$

$$\overline{\Gamma, x : X, \Gamma' \vdash x : X}$$

$$\overline{\Gamma \vdash () : 1}$$

$$\frac{\Gamma, x : X \vdash M : Y! \mathcal{C}}{\Gamma \vdash \text{fun } (x : X) \mapsto M : X \rightarrow Y! \mathcal{C}}$$

$$\frac{\Gamma \vdash V : X \rightarrow Y! \mathcal{C} \quad \Gamma \vdash W : X}{\Gamma \vdash VW : Y! \mathcal{C}}$$

$$\frac{\Gamma \vdash V : X}{\Gamma \vdash \text{return } V : X! \mathcal{C}}$$

$$\frac{\Gamma \vdash M : X! \mathcal{C} \quad \Gamma, x : X \vdash N : Y! \mathcal{C}}{\Gamma \vdash \text{let } x = M \text{ in } N : Y! \mathcal{C}}$$

$$\frac{\Gamma \vdash V : X}{\Gamma \vdash \langle V \rangle : \langle X \rangle}$$

$$\frac{\Gamma \vdash V : \langle X \rangle \quad \Gamma, x : X \vdash M : Y! \mathcal{C}}{\Gamma \vdash \text{await } V \text{ until } \langle x \rangle \text{ in } M : Y! \mathcal{C}}$$

$$\mathcal{C} = (o, l)$$

$$o = \{\text{op}_1, \dots, \text{op}_m\}$$

$$l = \{\text{op}'_1 \mapsto \mathcal{C}_1, \dots, \text{op}'_n \mapsto \mathcal{C}_n\}$$

$$l_{p_1} = \{\text{ping} \mapsto (\{\text{pong}\}, \emptyset)\}$$

$$l_p = \{\text{ping} \mapsto (\{\text{pong}\}, l_p)\}$$

$$l_m = \left\{ \text{stop} \mapsto \left(\emptyset, \{\text{go} \mapsto (\emptyset, l_m)\} \right) \right\}$$

$$\frac{\text{op} \in o \quad \Gamma \vdash V : A_{\text{op}} \quad \Gamma \vdash M : X!(o, \iota)}{\Gamma \vdash \textcolor{red}{\uparrow} \text{op} (V, M) : X!(o, \iota)}$$

$$\iota(\text{op}) = \mathcal{C}$$

$$\Gamma, x : A_{\text{op}} \vdash M : \langle X \rangle ! \mathcal{C}$$

$$\Gamma, p : \langle X \rangle \vdash N : Y!(o, \iota)$$

$$\Gamma \vdash \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } N : Y!(o, \iota)$$

$$\frac{\Gamma \vdash V : A_{\text{op}} \quad \Gamma \vdash M : X! \mathcal{C}}{\Gamma \vdash \textcolor{red}{\downarrow} \text{op} (V, M) : X! (\text{op} \textcolor{red}{\downarrow} \mathcal{C})}$$

$$\text{op} \textcolor{red}{\downarrow} (o, l) = \begin{cases} (o \cup o', l|_{\text{op}' \neq \text{op}} \cup l') & l(\text{op}) = (o', l') \\ (o, l) & \text{otherwise} \end{cases}$$

progress

$\vdash M : X!\mathcal{C}$

$\implies M \rightsquigarrow M' \quad \vee \quad M \text{ is final}$

$\Gamma \vdash M : X!\mathcal{C} \quad \wedge \quad M \rightsquigarrow M'$

$\implies \Gamma \vdash M' : X!\mathcal{C}$

preservation

progress

$\vdash M : X!\mathcal{C}$

$\Rightarrow M \rightsquigarrow M' \quad \vee \quad M \text{ is final}$



$\Gamma \vdash M : X!\mathcal{C} \quad \wedge \quad M \rightsquigarrow M'$

$\Rightarrow \Gamma \vdash M' : X!\mathcal{C}$

preservation

progress

$\vdash M : X!\mathcal{C}$

$\Rightarrow M \rightsquigarrow M' \quad \vee \quad M \text{ is final}$



$\Gamma \vdash M : X!\mathcal{C} \quad \wedge \quad M \rightsquigarrow M'$

$\Rightarrow \Gamma \vdash M' : X!\mathcal{C}$



preservation

TYPES

$$\Gamma \vdash V : X$$
$$\Gamma \vdash M : X!(o, l)$$

PROCESSES

run M $P \parallel Q$

$\uparrow \text{op}(V, P)$ $\downarrow \text{op}(V, P)$

$$\frac{M \rightsquigarrow N}{\text{run } M \rightsquigarrow \text{run } N}$$

$$\frac{P \rightsquigarrow Q}{\mathcal{F}[P] \rightsquigarrow \mathcal{F}[Q]}$$

$$\mathcal{F} ::= [] \mid \mathcal{F} \parallel Q \mid P \parallel \mathcal{F} \\ \mid \uparrow \text{op}(V, \mathcal{F}) \mid \downarrow \text{op}(V, \mathcal{F})$$

$$\text{run } (\uparrow \text{op } (V, M)) \rightsquigarrow \uparrow \text{op } (V, \text{run } M)$$

$$\uparrow \text{op } (V, P) \parallel Q \rightsquigarrow \uparrow \text{op } (V, P \parallel \downarrow \text{op } (V, Q))$$

$$P \parallel \uparrow \text{op } (V, Q) \rightsquigarrow \uparrow \text{op } (V, \downarrow \text{op } (V, P) \parallel Q)$$

$$\downarrow \text{op} (V, \text{run } M) \rightsquigarrow \text{run} (\downarrow \text{op} (V, M))$$

$$\downarrow \text{op} (V, P \parallel Q) \rightsquigarrow \downarrow \text{op} (V, P) \parallel \downarrow \text{op} (V, Q)$$

$$\downarrow \text{op} (V, \uparrow \text{op}' (W, P)) \rightsquigarrow \uparrow \text{op}' (W, \downarrow \text{op} (V, P))$$

demo

demo

$$M_i \rightsquigarrow M'_i$$

$$M_1 \parallel \cdots \parallel M_i \parallel \cdots \parallel M_n \rightsquigarrow M_1 \parallel \cdots \parallel M'_i \parallel \cdots \parallel M_n$$

demo

$$\begin{array}{c}
 M_i \rightsquigarrow M'_i \\
 \hline
 M_1 \parallel \cdots \parallel M_i \parallel \cdots \parallel M_n \rightsquigarrow M_1 \parallel \cdots \parallel M'_i \parallel \cdots \parallel M_n \\
 \\
 M_1 \parallel \cdots \parallel \uparrow \text{op}(V, M_i) \parallel \cdots \parallel M_n \\
 \rightsquigarrow \downarrow \text{op}(V, M_1) \parallel \cdots \parallel M'_i \cdots \parallel \downarrow \text{op}(V, M_n)
 \end{array}$$

$$\frac{\Gamma \vdash M : X!(o, \iota)}{\Gamma \vdash \text{run } M : X!!(o, \iota)}$$

$$\frac{\Gamma \vdash P : C \quad \Gamma \vdash Q : D}{\Gamma \vdash P \parallel Q : C \parallel D}$$

$$\frac{\text{op} \in \text{signals}(C) \quad \Gamma \vdash V : A_{\text{op}} \quad \Gamma \vdash P : C}{\Gamma \vdash \uparrow \text{op}(V, P) : C}$$

$$\frac{\Gamma \vdash V : A_{\text{op}} \quad \Gamma \vdash P : C}{\Gamma \vdash \downarrow \text{op} (V, P) : \text{op} \downarrow C}$$

$$\text{op} \downarrow (X!!(o, \iota)) = X!!(\text{op} \downarrow (o, \iota))$$

$$\text{op} \downarrow (C \parallel D) = (\text{op} \downarrow C) \parallel (\text{op} \downarrow D)$$

progress

$\vdash P : C$

$\implies P \rightsquigarrow P' \quad \vee \quad P \text{ is final}$

$\Gamma \vdash P : C \quad \wedge \quad P \rightsquigarrow P'$

$\implies \Gamma \vdash P' : C$

preservation

progress

$\vdash P : C$

$\Rightarrow P \rightsquigarrow P' \quad \vee \quad P \text{ is final}$



$\Gamma \vdash P : C \quad \wedge \quad P \rightsquigarrow P'$

$\Rightarrow \Gamma \vdash P' : C$

preservation

progress

$\vdash P : C$

$\Rightarrow P \rightsquigarrow P' \quad \vee \quad P \text{ is final}$



$\Gamma \vdash P : C \quad \wedge \quad P \rightsquigarrow P'$

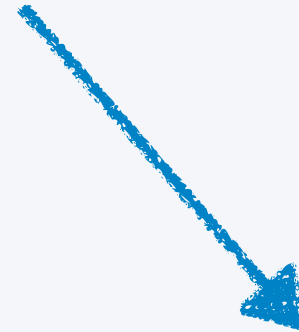
$\Rightarrow \Gamma \vdash P' : C$



preservation

$$\uparrow \text{op}(V, P) \parallel Q \rightsquigarrow \uparrow \text{op}(V, P \parallel \downarrow \text{op}(V, Q))$$

additional effects of
triggered handlers



$$\uparrow \text{op}(V, P) \parallel Q \rightsquigarrow \uparrow \text{op}(V, P \parallel \downarrow \text{op}(V, Q))$$

$$\overline{X!!(o, l) \rightsquigarrow X!!(o, l)}$$

$$\overline{X!!\text{ops} \downarrow (o, l) \rightsquigarrow X!!\text{ops} \downarrow (\text{op} \downarrow (o, l))}$$

$$\frac{C \rightsquigarrow C' \quad D \rightsquigarrow D'}{C \parallel D \rightsquigarrow C' \parallel D'}$$

progress

$\vdash P : C$

$\implies P \rightsquigarrow P' \quad \vee \quad P \text{ is final}$

$\Gamma \vdash P : C \quad \wedge \quad P \rightsquigarrow P'$

$\implies \exists C'. C \rightsquigarrow C' \quad \wedge \quad \Gamma \vdash P' : C'$

preservation

progress

$\vdash P : C$

$\Rightarrow P \rightsquigarrow P' \quad \vee \quad P \text{ is final}$



$\Gamma \vdash P : C \quad \wedge \quad P \rightsquigarrow P'$

$\Rightarrow \exists C'. C \rightsquigarrow C' \quad \wedge \quad \Gamma \vdash P' : C'$

preservation

progress

$\vdash P : C$

$\Rightarrow P \rightsquigarrow P' \quad \vee \quad P \text{ is final}$



$\Gamma \vdash P : C \quad \wedge \quad P \rightsquigarrow P'$

$\Rightarrow \exists C'. C \rightsquigarrow C' \quad \wedge \quad \Gamma \vdash P' : C'$

preservation



PROCESSES

run M $P \parallel Q$

$\uparrow \text{op}(V, P)$ $\downarrow \text{op}(V, P)$

EXTENSIONS

$$\mathcal{C} \sqsubseteq \iota(\text{op}) \quad \Gamma, p : \langle X \rangle \vdash N : Y!(o, \iota)$$

$$\Gamma, x : A_{\text{op}}, r : 1 \rightarrow \langle X \rangle ! (\emptyset, \{\text{op} \mapsto \mathcal{C}\}) \vdash M : \langle X \rangle ! \mathcal{C}$$

$$\Gamma \vdash \text{promise } (\text{op } x \ r \mapsto M) \text{ as } p \text{ in } N : Y!(o, \iota)$$


$$\downarrow \text{op } (V, \text{promise } (\text{op } x \ r \mapsto M) \text{ as } p \text{ in } N)$$

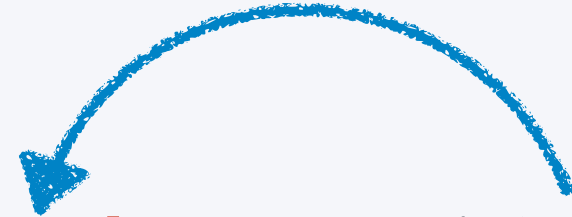
$$\rightsquigarrow \text{let } p = M[V/x, R/r] \text{ in } \downarrow \text{op } (V, N)$$

$$\text{where } R = \text{fun } () \mapsto \text{promise } (\text{op } x \ r \mapsto M) \text{ as } p \text{ in return } p$$

promise (op $x \mapsto M$) **as** p **in** \uparrow op' (V, N)
 $\rightsquigarrow \uparrow$ op' (V , **promise** (op $x \mapsto M$) **as** p **in** N)

$\text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } \uparrow \text{op}'(V, N)$
 $\rightsquigarrow \uparrow \text{op}'(V, \text{promise } (\text{op } x \mapsto M) \text{ as } p \text{ in } N)$





promise (op $x \mapsto M$) **as** p **in** \uparrow op' (V, N)

\rightsquigarrow \uparrow op' (V , **promise** (op $x \mapsto M$) **as** p **in** N)

**PROMISE VARIABLES CAN'T
ESCAPE THROUGH SIGNAL PAYLOADS**

**IF YOUR TYPE SYSTEM
RESTRICTS PAYLOADS TO GROUND TYPES**

$$A, B ::= b \mid 1 \mid 0 \mid A \times B \mid A + B$$

$$X, Y ::= A \mid X \times Y \mid X + Y \mid$$

$$X \rightarrow Y!(o, \iota) \mid \langle X \rangle$$

$$\frac{\text{op} \in o \quad \Gamma \vdash V : A_{\text{op}} \quad \Gamma \vdash M : X!(o, \iota)}{\Gamma \vdash \textcolor{red}{\uparrow} \text{op} (V, M) : X!(o, \iota)}$$

$$A, B ::= \mathbf{b} \mid 1 \mid 0 \mid A \times B \mid A + B \mid [X]$$

$$X, Y ::= A \mid X \times Y \mid X + Y \mid$$

$$X \rightarrow Y!(o, \iota) \mid \langle X \rangle \mid [X]$$

$$\frac{\text{op} \in o \quad \Gamma \vdash V : A_{\text{op}} \quad \Gamma \vdash M : X!(o, \iota)}{\Gamma \vdash \textcolor{red}{\uparrow} \text{op} (V, M) : X!(o, \iota)}$$

$$X \text{ is mobile} \quad \text{or} \quad \blacksquare \notin \Gamma'$$

$$\Gamma, x : X, \Gamma' \vdash x : X$$
$$\Gamma, \blacksquare \vdash V : X$$

$$\Gamma \vdash [V] : [X]$$
$$\Gamma \vdash V : [X]$$
$$\Gamma, x : X \vdash M : Y! \mathcal{C}$$

$$\Gamma \vdash \text{unbox } V \text{ as } [x] \text{ in } M : Y! \mathcal{C}$$
$$\text{unbox } [V] \text{ as } [x] \text{ in } M \rightsquigarrow M[V/x]$$

$\text{run } (\text{spawn } (M, N)) \rightsquigarrow \text{run } M \parallel \text{run } N$

$$\frac{\Gamma, \blacksquare \vdash M : X!\mathcal{C} \quad \Gamma \vdash N : Y!\mathcal{C}'}{\Gamma \vdash \text{spawn } (M, N) : Y!\mathcal{C}'}$$

$\text{let } x = (\text{spawn } (M_1, M_2)) \text{ in } N$
 $\rightsquigarrow \text{spawn } (M_1, \text{let } x = M_2 \text{ in } N)$

$\text{promise } (\text{op } x \ r \mapsto M) \text{ as } p \text{ in spawn } (N_1, N_2)$
 $\rightsquigarrow \text{spawn } (N_1, (\text{promise } (\text{op } x \ r \mapsto M) \text{ as } p \text{ in } N_2))$

$\downarrow \text{op } (V, \text{spawn } (M, N))$
 $\rightsquigarrow \text{spawn } (M, \downarrow \text{op } (V, N))$

let $x = (\text{spawn } (M_1, M_2))$ **in** N

\rightsquigarrow **spawn** $(M_1, \text{let } x = M_2 \text{ in } N)$

\nwarrow algebraicity

promise $(\text{op } x \ r \mapsto M)$ **as** p **in** **spawn** (N_1, N_2)

\rightsquigarrow **spawn** $(N_1, (\text{promise } (\text{op } x \ r \mapsto M)$ **as** p **in** $N_2))$

\nwarrow commutativity

\downarrow **op** $(V, \text{spawn } (M, N))$

\rightsquigarrow **spawn** $(M, \downarrow \text{op } (V, N))$

\nwarrow "handling"

demo

EXTENSIONS

INTERESTED?



Asynchronous Effects

DANEL AHMAN and MATIJA PRETNAR, University of Ljubljana, Slovenia

We explore asynchronous programming with algebraic effects. We complement their conventional synchronous treatment by showing how to naturally also accommodate asynchrony within them, namely, by decoupling the execution of operation calls into signalling that an operation's implementation needs to be executed, and interrupting a running computation with the operation's result, to which the computation can react by installing interrupt handlers. We formalise these ideas in a small core calculus, called λ_{ae} . We demonstrate the flexibility of λ_{ae} using examples ranging from a multi-party web application, to preemptive multi-threading, to remote function calls, to a parallel variant of runners of algebraic effects. In addition, the paper is accompanied by a formalisation of λ_{ae} 's type safety proofs in AGDA, and a prototype implementation of λ_{ae} in OCAML.

CCS Concepts: • **Theory of computation** → **Concurrency**; **Program constructs**; **Program semantics**.

Additional Key Words and Phrases: algebraic effects, asynchrony, concurrency, interrupt handling, signals.

ACM Reference Format:

Danel Ahman and Matija Pretnar. 2021. Asynchronous Effects. *Proc. ACM Program. Lang.* 5, POPL, Article 24 (January 2021), 28 pages. <https://doi.org/10.1145/3434305>

1 INTRODUCTION

Effectful programming abstractions are at the heart of many modern general-purpose programming languages. They can increase expressiveness by giving access to first-class continuations, but often simply help users to write cleaner code, e.g., by avoiding having to manage a program's memory explicitly in state-passing style, or getting lost in callback hell while programming asynchronously.

An increasing number of language designers and programmers are starting to embrace *algebraic effects*, where one uses algebraic operations [Plotkin and Power 2002] and effect handlers [Plotkin and Pretnar 2013] to uniformly and user-definably express a wide range of effectful behaviour, ranging from basic examples such as state, rollbacks, exceptions, and nondeterminism [Bauer and Pretnar 2015], to advanced applications in concurrency [Dolan et al. 2018] and statistical probabilistic programming [Bingham et al. 2019], and even quantum computation [Staton 2015].

While covering many examples, the conventional treatment of algebraic effects is *synchronous* by nature. In it effects are invoked by placing operation calls in one's code, which then propagate outwards until they trigger the actual effect, finally yielding a result to the rest of the computation that has been *waiting* the whole time. While blocking the computation is indeed sometimes needed, e.g., in the presence of general effect handlers that can execute their continuation any number of times, it forces all uses of algebraic effects to be synchronous, even when this is not necessary, e.g., when the effect involves executing a remote query to which a response is not needed (immediately).

Motivated by the recent interest in the combination of asynchrony and algebraic effects [Dolan et al. 2018; Leijen 2017], we explore what it takes (in terms of language design, safe programming abstractions, and a self-contained core calculus) to accompany the synchronous treatment of

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<https://doi.org/10.1145/3434305>

HIGHER-ORDER ASYNCHRONOUS EFFECTS*

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ABSTRACT. We explore asynchronous programming with algebraic effects. We complement their conventional synchronous treatment by showing how to naturally also accommodate asynchrony within them, namely, by decoupling the execution of operation calls into signalling that an operation's implementation needs to be executed, and interrupting a running computation with the operation's result, to which the computation can react by installing interrupt handlers. We formalise these ideas in a small core calculus, called λ_{ae} . We demonstrate the flexibility of λ_{ae} using examples ranging from a multi-party web application, to preemptive multi-threading, to remote function calls, to a parallel variant of runners of algebraic effects. In addition, the paper is accompanied by a formalisation of λ_{ae} 's type safety proofs in AGDA, and a prototype implementation of λ_{ae} in OCAML.

1. INTRODUCTION


Effectful programming abstractions are at the heart of many modern general-purpose programming languages. They can increase expressiveness by giving access to first-class continuations, but often simply help users to write cleaner code, e.g., by avoiding having to manage a program's memory explicitly in state-passing style, or getting lost in callback hell while programming asynchronously.

An increasing number of language designers and programmers are starting to embrace *algebraic effects*, where one uses algebraic operations [PP02] and effect handlers [PP13] to uniformly and user-definably express a wide range of effectful behaviour, ranging from basic examples such as state, rollbacks, exceptions, and nondeterminism [BP15], to advanced applications in concurrency [DEH⁺18] and statistical probabilistic programming [BCJ⁺19], and even quantum computation [Sta15].

While covering many examples, the conventional treatment of algebraic effects is *synchronous* by nature. In it effects are invoked by placing operation calls in one's code, which

Key words and phrases: algebraic effects, asynchrony, concurrency, interrupt handling, signals.

* This paper is an extended version of our previous work [AP21], which simplifies the meta-theory, removes the reliance on general recursion for reinstallable interrupt handlers, extends the calculus with higher-order interrupt payloads and dynamic process creation, and strengthens the examples of application.

This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No 834146 . This material is based upon work supported by the Air Force Office of Scientific Research under awards number FA9550-17-1-0326 and FA9550-21-1-0024.

Before
submitting,
go through
LMCS check-
list

Create
LMCS Git
tags for Agda
and Agda



master

1 branch

1 tag

Go to file

Code

	license	71ebd9 on Oct 7, 2021	162 commits
	AEff.agda	merging value, computation, and process type modules	3 years ago
	AwaitingComputations.agda	removing unused lemmas and better naming conventions	3 years ago
	EffectAnnotations.agda	Proof-irrelevance of subtyping relations	3 years ago
	Finality.agda	Finality of result forms	3 years ago
	LICENSE.md	license	2 years ago
	Preservation.agda	Syncing a lemma annotation with the paper. Removing a spurious mu...	3 years ago
	ProcessFinality.agda	Tweaking the notation	3 years ago
	ProcessPreservation.agda	Tweaking the notation	3 years ago
	ProcessProgress.agda	Finality of process result forms	3 years ago
	Progress.agda	Syncing names with the paper	3 years ago
	README.md	Update README.md	2 years ago
	Renamings.agda	actions of renamings and substitutions for processes	3 years ago
	Substitutions.agda	actions of renamings and substitutions for processes	3 years ago
	Types.agda	Tweaking the notation	3 years ago

README.md

Agda formalisation of the AEff language

Note: For the Agda formalisation of a newer version of AEff (extended with reinstallable interrupt handlers, higher-order payloads for signals and interrupts, and dynamic process creation), see [here](#).

- The formalisation has been tested with Agda version 2.6.1 and standard library version 1.3.
- The unicode symbols used in the source code have tested to display correctly with the DejaVu Sans Mono

About

Agda formalisation of the AEff language

Readme

MIT license

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Report repository

Releases 1

POPL 2021 Latest
on Nov 10, 2020

Packages

No packages published

Languages

Agda 100.0%



main 1 branch 0 tags

Go to file

Code

danelahman	license	b41df71 on Oct 7, 2021	36 commits
AEff.agda	removing let-rec from the core calculus	2 years ago	
EffectAnnotations.agda	Removing a redundant mutual block	2 years ago	
Finality.agda	removing the separate judgement of awaiting computations (not nee...	2 years ago	
LICENSE.md	license	2 years ago	
Preservation.agda	removing let-rec from the core calculus	2 years ago	
ProcessFinality.agda	for symmetry, allow type-level spawning both in left and right	2 years ago	
ProcessPreservation.agda	for symmetry, allow type-level spawning both in left and right	2 years ago	
ProcessProgress.agda	removing the separate judgement of awaiting computations (not nee...	2 years ago	
Progress.agda	removing the separate judgement of awaiting computations (not nee...	2 years ago	
README.md	Update README.md	2 years ago	
Renamings.agda	removing let-rec from the core calculus	2 years ago	
Substitutions.agda	removing let-rec from the core calculus	2 years ago	
Types.agda	wip: reinstallable interrupt handlers (up to coercion rules)	2 years ago	

README.md

Agda formalisation of the AEff language for higher-order asynchronous effects

- The core language formalised here differs from the [original language](#) as follows:
 - interrupt handlers are now able to reinstall themselves (without resorting to general let-rec);
 - payloads of signals/interrupts have been generalised to allow higher-order values (by the means of modal types);

About

No description, website, or topics provided.

Readme

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Releases

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Packages

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Contributors 2

danelahman Danel Ahman

matijapretnar Matija Pretnar

Languages

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master

3 branches

1 tag

Go to file

Code

	license	3af50c5 on Oct 7, 2021	135 commits
	.github/workflows	Fix ocamlformat version	2 years ago
	etc	-> ~> ->	2 years ago
	examples	Add dynamic creation of processes	2 years ago
	src	Improve checking of mobile type definitions	2 years ago
	tests	Improve checking of mobile type definitions	2 years ago
	web	Simplify styles	3 years ago
	.gitignore	Provide a command-line backend	3 years ago
	.ocamlformat	Enable OCamlFormat	3 years ago
	LICENSE.md	license	2 years ago
	Makefile	Add testing framework	3 years ago
	README.md	Update README.md	2 years ago
	dune-project	Switch to dune	3 years ago

README.md

Æff

Install dependencies by

```
opam install menhir ocaml-vdom ocamlformat
```

and build Æff by running (requires OCaml >= 4.08.0)

```
make
```

About

An interactive interpreter for asynchronous algebraic effects

matija.pretnar.info/aeff/

Readme

MIT license

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Report repository

Releases 1

POPL 2021 Latest
on Nov 10, 2020

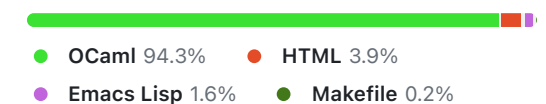
Packages

No packages published

Contributors 3

- matijapretnar Matija Pretnar
- danelahman Danel Ahman
- JanezRadescek

Languages





main

4 branches 0 tags

Go to file

Code



matijapretnar Bump OCaml & ocamlformat version

✓ f28a4ba on Nov 16, 2022 43 commits

.github/workflows	Bump OCaml & ocamlformat version	7 months ago
examples	Initial commit	3 years ago
src	Bump OCaml & ocamlformat version	7 months ago
tests	Check for well-formed type definitions	2 years ago
web	Sort out names	2 years ago
.gitignore	Sort out names	2 years ago
.ocamlformat	Bump OCaml & ocamlformat version	7 months ago
Makefile	Simplify test folder	2 years ago
README.md	Bump OCaml & ocamlformat version	7 months ago
dune-project	Add initial cram tests setup	2 years ago

README.md

Millet

Do you, like me, test theoretical programming language concepts by building your own programming language? Do you, like me, do it by copying and modifying your most recent language because you are too lazy to build everything from scratch? Do you, like me, end up with a mess? Then Millet is for you. It is a pure ML-like language with simple and modular codebase that you can use as a template for your next language.

How to install and run Millet?

Install dependencies by

```
opam install menhir ocaml-vdom ocamlformat
```

About

A ML-like pure functional language that can be used as a template for creating your own language

matija.pretnar.info/millet/

Readme

19 stars

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Report repository

Releases

No releases published

Packages

No packages published

Contributors 2

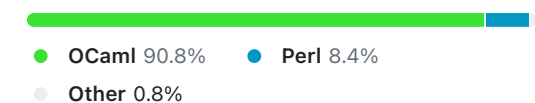


matijapretnar Matija Pretnar



zputrle Žiga Putrle

Languages



FUTURE WORK

EFFICIENT **INTERPRETER**

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DENOTATIONAL

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QUESTIONS?